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Full length article Biaxial mechanics of thermally denaturing skin - Part 2: Modeling

Manuel Rausch^{a,b,c}, William D. Meador^a, John Toaquiza-Tubon^d, Omar Moreno-Flores^d, Adrian Buganza Tepole^{d,e,*}

^a Department of Biomedical Engineering, The University of Texas at Austin, Austin, TX, 78712, USA

^b Department of Aerospace Engineering and Engineering Mechanics, The University of Texas at Austin, Austin, TX, 78712, USA

^c Oden Institute for Computational Engineering and Sciences, The University of Texas at Austin, Austin, TX, 78712, USA

^d School of Mechanical Engineering, Purdue University, West Lafayette, IN, 47907, USA

e Weldon School of Biomedical Engineering, Purdue University, West Lafayette, IN, 47907, USA

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ABSTRACT

Understanding the response of skin to superphysiological temperatures is critical to the diagnosis and prognosis of thermal injuries, and to the development of temperature-based medical therapeutics. Unfortunately, this understanding has been hindered by our incomplete knowledge about the nonlinear coupling between skin temperature and its mechanics. In Part I of this study we experimentally demonstrated a complex interdependence of time, temperature, direction, and load in skin's response to superphysiological temperatures. In Part II of our study, we test two different models of skin's thermomechanics to explain our observations. In both models we assume that skin's response to superphysiological temperatures is governed by the denaturation of its highly collageneous microstructure. Thus, we capture skin's native mechanics via a microstructurally-motivated strain energy function which includes probability distributions for collagen fiber orientation and waviness. In the first model, we capture skin's response to superphysiological temperatures as a transition between two states that link the kinetics of collagen fiber denaturation to fiber coiling and to the transformation of each fiber's constitutive behavior from purely elastic to viscoelastic. In the second model, we capture skin's response to superphysiological temperatures instead via three states in which a sequence of two reactions link the kinetics of collagen fiber denaturation to fiber coiling, followed by a state of fiber damage. Given the success of both models in qualitatively and quantitatively capturing our observations, we expect that our work will provide guidance for future experiments that could probe each model's assumptions toward a better understanding of skin's coupled thermo-mechanics and that our work will be used to guide the engineering design of heat treatment therapies.

Statement of significance

Quantifying and modeling skin thermo-mechanics is critical to our understanding of skin physiology, pathophysiology, as well as heat-based treatments. This work addresses a lack of theoretical and computational models of the coupled thermo-mechanics of skin. Our model accounts for skin microstructure through modeling the probability of fiber orientation and fiber stress-free states. Denaturing induces changes in the stress-free configuration of collagen, as well as changes in fiber stiffness and viscoelastic properties. We propose two competing models that fit all of our experimental observations. These models will enable future developments of thermal-therapeutics, prevention and management of skin thermal injuries, and set a foundation for improved mechanistic models of skin thermo-mechanics.

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1. Introduction

Life is highly temperature sensitive with even the most welladapted metazoans succumbing to temperatures beyond 50 °C [1]. Indeed, mammals thermo-regulate within a very narrow body temperature range of 30-40 °C. Beyond these temperatures, vital

E-mail address: abuganza@purdue.edu (A.B. Tepole).

Corresponding author.





proteins, such as the ubiquitous structural protein collagen, thermally denature [2]. That is, collagen's complex hierarchical organization disassociates. As collagen breaks down, so do the tissues whose microstructure is governed by collagen [3,4]. The exact mechanisms that link collagen denaturation to those tissues' thermo-mechanical response to superphysiological temperatures are not fully understood. However, our current understanding is that the breaking of collagen's inter- and intra-molecular bonds from exposure to superphysiological temperatures leads to an energetically more favorable coiled state, i.e., a reduction in the collagen molecule reference length. Loss of cross-links also leads to a reduced load-bearing capacity of collagen [5–7]. As a result, at the macroscopic scale, superphysiological temperature loading shrinks collageneous tissues and changes their characteristic Jshape stress-strain curve into a more linear behavior. Ultimately, once collagen is fully denatured, collageneous tissues take a gelatinous form and lose their mechanical integrity completely [8–10].

Collagen is a critical constituent that supports connective tissues such as skin. In turn, understanding thermal denaturation of skin is important to understand the pathophysiology of thermal injury, such as the one million burn wounds that are treated each year in the US alone [11,12]. Understanding skin's response to superphysiological temperatures is also important for the development of temperature-dependent therapeutics. For example, laser therapy has emerged as an effective treatment for scar tissue [13]. Despite the importance of understanding skin's response to thermal loading, many gaps in knowledge remain. Among them, we currently lack comprehensive knowledge of the relationship between superphysiological temperatures and skin's mechanical behavior. In Part I of this study, we aimed at filling some of these gaps and concluded that thermal treatment of skin above 55 °C results in time-, temperature-, and direction-dependent shrinkage under isotonic traction-free conditions. Similarly, we found that thermal treatment of skin above 55 °C results in time-, temperature-, and direction-dependent force production under isometric conditions. Additionally, we concluded that thermal treatment of skin results in stiffening and softening of skin at low and high strains, respectively. Supported by histology and second harmonic generation imaging, we also demonstrated that these thermo-mechanical phenomena are driven by the denaturation of collagen. Our work thus confirmed and built on others' previous work on the thermo-mechanical coupling of denaturing, collageneous soft tissues. For example, Chen at al. subjected chordae tendineae to different thermo-mechanical loading conditions and observed that tissue shrinkage and force production demonstrated time-temperature-load equivalence [10,14]. Similarly, Harris et al. and Baek et al. found that epicardium exhibited a less pronounced strain-stiffening response after thermal treatment than before [9,15]. Similar observations were made by Boronyak et al. and Bender et al. after radio-frequency ablation of valvular tissue [16,17]. Finally, skin-specific work by Zhou et al. and Xu et al. showed, comparably to our findings, that the modulus of the tissue decreased after thermal treatment and that its viscoelastic response became more pronounced [8,18]. Capturing above observations in quantitative models is a critical element in generating and testing hypotheses that can explain the origins of these observations.

There have been previous efforts toward such quantitative models [18–20]. While each of those models captured some elements of the complex, coupled interplay between thermal treatment and mechanics, none can comprehensively explain time-, temperature, direction-, and load-dependent observations that experimental studies have identified. Part II of our study tests competing models of skin's response to superphysiological temperatures that can explain ours and others' recent experimental observations on the coupled thermo-mechanics of denaturing collageneous

tissues with a specific focus on skin [21]. Our models build on the well-established Arrhenius-type kinetics of collagen denaturation [22]. We specifically aim at linking these kinetics to denaturationinduced changes on the tissue scale such as shrinkage, change in mechanical properties, change in viscoelastic properties and/or damage. To this end, we extend previous modeling efforts and propose two competing models. In both models, we consider collagen the primary, structural constituent of skin. Note, as a first approximation we ignore the multi-layered structure of skin that is comprised of the outermost epidermis, the collagenous and load-bearing dermis, and the adipose hypodermis. Similarly, we ignore spatial heterogeneities such as hair follicles or vasculature [23]. Also note that we assume collagen denaturation drives the thermo-mechanical response of skin to superphysiological temperatures. To this end, we introduce a constitutive model of intact skin that captures the tissue's nonlinear and anisotropic response by explicitly modeling the collagen fiber orientation and waviness distributions. In our first model, we consider collagen, and thus skin, denaturation as a two-state phenomenon where the denatured collagen changes its reference configuration and becomes viscoelastic. In our second model, we consider collagen denaturation as a three-state phenomenon in which no viscoelasticity is assumed. Instead, the denaturation process is split into two steps: an intermediate state of collagen molecules with a reduced stressfree length before a final, damaged state in which the collagen molecules and fibrils cannot carry mechanical load. Both implementations are schematized in Fig. 1 and were also motivated by Buehler [24,25].

2. Materials and Methods

2.1. Mechanics of intact skin

We model the native state of skin as a hyperelastic, constrained mixture with contributions to the strain energy from an isotropic matrix, W^{m} , and distributed collagen fibers, \hat{W}^{f} . To this end, we characterize the local deformation by the deformation gradient F and express the strain energy as a function of the right Cauchy-Green deformation tensor $\mathbf{C} = \mathbf{F}^{\top} \mathbf{F}$. Specifically, we capture the contribution of the isotropic matrix via the deformation tensor's first invariant $I_1 = \mathbf{C}$: I. In contrast to the common approach of capturing collagen's contribution to the strain energy via a condensation into a single pseudo-invariant [23,26], we choose a microstructurally-inspired approach [27-29]. The contribution of a single fiber in the \mathbf{a}_0 's material direction to the strain energy is through its pseudo-invariant $I_4(\theta) = \mathbf{C} : \mathbf{a}_0(\theta) \otimes \mathbf{a}_0(\theta)$. The total contribution of all fibers to the strain energy, \hat{W}^{f} , thus follows from integration across the contributions of each individual fiber at angle θ , $W^{f}(\theta)$, according to their probability density distribution $\rho^{\theta}(\theta)$. Throughout this work, we also assume that skin behaves incompressibly, a common assumption for soft collageneous tissues [30], which we enforce via the Lagrange-multiplier *p*. The total strain energy function consequently reads

$$W(\mathbf{C}) = W^{\mathrm{m}}(\mathbf{C}) + \hat{W}^{\mathrm{f}}(\mathbf{C}) + p[J-1], \qquad (1)$$

with

$$\hat{W}^{f}(\mathbf{C}) = \int \rho^{\theta}(\theta) W^{f}(\mathbf{C}, \theta) d\theta.$$
(2)

Here we approximate the matrix behavior as neo-Hookean

$$W^{\rm m}(\mathbf{C}) = \mu^{\rm m}[I_1 - 3]/2,$$
 (3)

with μ^{m} being its shear modulus. In addition to capturing collagen's distributed orientation, we also capture the distribution of its waviness, which is a microstructural characteristic of collagen in skin and other soft tissues. To this end, we introduce the waviness

A Intact skin



Fig. 1. Competing models of skin's thermo-mechanical response to superphysiological temperatures. A) Independent of the model, we approximate intact skin's constitutive behavior as hyperelastic, where the strain energy function is microstructurally-inspired by explicitly considering probability distributions of collagen orientation and waviness. B) The two-state model predicts thermally-induced changes in skin's mechanical properties via one reaction that simultaneously induces two changes: i) a transition in the stress-free reference configuration toward a smaller (coiled) collagen length which is captured by a translation of the waviness distribution; ii) inclusion of viscoelasticity in the collagen behavior which we argue is due to inter- and intra-fibrillar bonds disassociating; thus, enabling relative sliding within and between fibers. C) The three-state model predicts thermally-induced changes in the mechanical properties of denaturing skin via two subsequent reactions: i) initially, we argue that denaturation leads to coiling of collagen molecules that we, again, capture through a translation of the collagen waviness distribution; ii) in a second reaction, we argue that continued disassociation of cross-links leads to loss of collagen's strain energy storage capacity, i.e., reduction in material stiffness or damage.

distribution $\rho^{\lambda s}(\lambda_s)$, where λ_s may be interpreted as a distributed reference length [29,31]. That is, while the fiber is crimped we assume it does not provide resistance to stretch and only does so once uncrimped. Consequently, the stretch-induced energy contribution of each fiber, W^f , follows from its relative orientation, via θ , and its individual reference length, via λ_s , viz.

$$W^{\rm f}(\mathbf{C},\theta) = \mu^{\rm f} \int \rho^{\lambda_{\rm s}}(\lambda_{\rm s}) \left[\bar{\lambda}^2 + 2\bar{\lambda}^{-1} - 3\right] \mathrm{d}\lambda_{\rm s}\,,\tag{4}$$

where $\lambda = \lambda(\mathbf{C}, \theta)$ is the macroscopic stretch in the θ -direction, i.e., the square root of the pseudo-invariant $I_4(\theta) = \mathbf{C} : \mathbf{a}_0(\theta) \otimes \mathbf{a}_0(\theta)$, and $\overline{\lambda} = \lambda/\lambda_s$ is the fiber stretch relative to its respective

reference length. The description of each fiber's strain energy contribution is that of a neo-Hookean cylinder under uniaxial extension and with traction-free boundaries. In our model, each collagen fiber's constitutive behavior is thus determined by a single material parameter, its shear modulus $\mu^{\rm f}$. However, its contribution to the total strain energy depends also on its orientation and its reference length.

The second Piola-Kirchhoff stress tensor for intact skin then follows from the Clausius-Duhem inequality as

$$\mathbf{S} = 2\frac{\partial W}{\partial \mathbf{C}} = \mu^{m}\mathbf{I} + \int \rho^{\theta}\mathbf{S}^{\mathrm{f}}\mathrm{d}\theta + p\mathbf{C}^{-1}, \qquad (5)$$

Table 1

Constitutive parameters of intact skin.

Matrix Stiffness	Collagen Stiffness	Orientation Parameters	Waviness Parameters		
μ^m [MPa]	μ^f [MPa]	κ[-]	β [-]	δ [-]	γ[-]
0.001	18.63	1.22	1.63	0.09	1.07

where we drop the dependencies on θ and **C** for convenience. The fiber contribution to the stress for each fiber, in turn, reads

$$\mathbf{S}^{\mathrm{f}} = 2 \frac{\partial W^{\mathrm{f}}}{\partial \mathbf{C}} = \mu^{\mathrm{f}} \lambda^{-2} \int \rho^{\lambda_{\mathrm{s}}} \left[\bar{\lambda}^{2} - \bar{\lambda}^{-1} \right] \mathrm{d}\lambda_{\mathrm{s}} \mathbf{a}_{0} \otimes \mathbf{a}_{0} \,. \tag{6}$$

Please note that we model skin as a thin membrane that fulfills the plane-stress condition. Accordingly, we model fibers only within this plane. Additionally, this assumption implies zero normal surface tractions and allows us to analytically solve for the Lagrange multiplier p.

For the orientation distribution function, ρ^{θ} , we consider a π -periodic von Mises distribution

$$\rho^{\theta}(\theta) = \frac{\exp\left(\kappa \left[\cos\left(2\theta - \hat{\theta}\right)\right]\right)}{2\pi I_0(\kappa)}, \qquad (7)$$

with concentration parameter κ , the mean fiber orientation $\hat{\theta}$, and with $I_0(\kappa)$ being the Bessel function of order zero. For the waviness distribution function, ρ^{λ_s} , we use the Weibull distribution

$$\rho^{\lambda_s}(\lambda_s) = \frac{\beta}{\delta} \left[\frac{\lambda_s - \gamma}{\delta} \right]^{\beta - 1} \exp\left(- \left[\frac{\lambda_s - \gamma}{\delta} \right]^{\beta} \right), \tag{8}$$

where the parameter γ controls the shift of the distribution along the abscissa, while β and δ are called the shape and scale parameters and control the skewness and width of the distribution, respectively. The orientation and waviness distribution for intact skin are illustrated in Fig. 1A.

As a first approximation for above parameters, we inform the stiffness parameters μ^{m} , μ^{f} , as well as the orientation distribution parameters κ from our previous work [32]. We additionally quantify manually the end-to-end and contour length of individual fibers in two-photon images reported in Part I and use these measurements to estimate the waviness distribution, see Supplementary Figures S1 and S2. Next, we optimize those parameters to match our baseline biaxial experiments on dorsal murine skin from Part I, see Supplemental Figure S2. The optimized parameters are reported in Table 1. Note that we assign $\hat{\theta}$ of the von Mises distribution equal to zero (i.e., in lateral direction).

2.2. Mathematical models of skin's response to superphysiological temperatures

In the design of both modeling approaches we set out to capture three heat-induced phenomena that we observed in Part I of this study. When heated, i) skin shrinks under traction-free conditions, ii) skin produces tractions that quickly decay when under isometric conditions, and iii) skin's constitutive behavior becomes stiffer at low strains and softer at high strains. The below models are built on competing assumptions as to the molecular mechanisms that lend them the ability to predict these phenomena. However, both models share the assumption that collagen and, therefore, collageneous soft tissue denature according to first order kinetics with Arrhenius-type rate, viz.

$$k_d = A \exp\left(-E_a/RT\right),\tag{9}$$

where k_d is the rate of denaturation, A is the maximum rate, E_a is the activation energy, R is the universal gas constant, and T

is the temperature. This assumption is based on previous work by Xu et al., for example, who measured $E_a = 5.867 \times 10^5$ J/mol and $A = 5.240 \times 10^{91}$ s⁻¹ [8], while Stylianopoulos identified A = 1.1363×10^{86} s⁻¹ and $E_a = 5.6233 \times 10^5$ J/mol [20], and Chen et al. measured $A = 1.3 \times 10^{53}$ s⁻¹ and $E_a = 3.57$ kJ/mol; see also the excellent review by Wright et al. [22].

2.2.1. Two-state model

In our first model, we propose that denaturation of collagen is governed by a transition from a native state to one denatured state. The ordinary differential equations (ODEs) describing this process are

$$\dot{C}_{o} = -k_{d}(T)C_{o}$$

$$\dot{C}_{d} = +k_{d}(T)C_{o},$$
(10)

where C_0 and C_d denote the concentration of native and denatured collagen respectively.

The second, non-native state is characterized by a reduction in collagen's reference (coiled) length and a transition from being a purely elastic material to being a viscoelastic material, see Fig. 1B. The first change in collagen's properties is motivated by the breaking of inter- and intra-molecular bonds that leads to the dissociation of the collagen triple helix and coiling of collagen molecules; we capture this change by a change in the fibers' waviness distribution. The second change in collagen's properties is motivated by the breaking of inter- and intra-molecular bonds that leads to relative sliding between collagen fibrils under load; we capture this change by altering the fibers' hyperelastic constitutive model to a hyper-viscoelastic one [33]. The strain energy of the mixture thus reads

$$W = W^{m} + C_{o} \int \rho^{\theta} W^{f} d\theta + C_{d} \int \rho^{\theta} W^{f,eq}_{d} d\theta + C_{d} \int \rho^{\theta} W^{f,visc}_{d} d\theta + p[J-1], \qquad (11)$$

where the subscript 'd' denotes quantities associated with denatured collagen and tissue. For example, $W_d^{f,eq}$ and $W_d^{f,visco}$ represent the damaged fibers' equilibrium contribution and a viscoelastic contributions to the strain energy function. Specifically,

$$W_{\rm d}^{\rm f,eq} = \mu_{\rm d}^{\rm f} \int \rho_{\rm d}^{\lambda_{\rm s}} \left[\bar{\lambda}^2 + 2\bar{\lambda}^{-1} - 3 \right] d\lambda_{\rm s}. \tag{12}$$

Here, again, note that the subscript 'd' in $\rho_d^{\lambda_s}$ and μ_d^f indicates that those quantities change during denaturation (4). Analogous to the equilibrium contribution, the viscoelastic contribution reads

$$W_{\rm d}^{\rm f,visc} = \phi \mu_{\rm d}^{\rm f} \int \rho_{\rm d}^{\lambda_{\rm s}} \left[(\bar{\lambda}^{\rm e})^2 + 2(\bar{\lambda}^{\rm e})^{-1} - 3 \right] \mathrm{d}\lambda_{\rm s}, \tag{13}$$

except that its evolution is driven by the elastic deformation of a Maxwell-type branch $\bar{\lambda}^e = \sqrt{J_4^e}/\lambda_s$ rather than the total stretch λ . Note, following [34,35] it is assumed that the viscoelastic part of the strain energy function is proportional to the equilibrium branch through the factor ϕ . The second Piola Kirchhoff stress tensor then follows from the Doyle-Erickson relation as

$$\mathbf{S} = \mu^{m} \mathbf{I} + C_{o} \int \rho^{\theta} \mathbf{S}^{f} d\theta + C_{d} \int \rho^{\theta} \mathbf{S}^{f,eq}_{d} d\theta + C_{d} \int \rho^{\theta} \mathbf{S}^{f,visc}_{d} d\theta + p \mathbf{C}^{-1}, \qquad (14)$$

where the fiber equilibrium and viscoelastic stresses, $\mathbf{S}_{d}^{f, eq}$ and $\mathbf{S}_{d}^{f, visc}$, respectively, are computed as in Eq. 6. For the update of the viscous strain, consider that the rate of change of the stress is proportional to the stress,

$$\dot{\mathbf{S}}_{d}^{f,\text{visc}} = -\frac{1}{\tau} \mathbf{S}_{d}^{f,\text{visc}} \,. \tag{15}$$

Table 2

Parameters for the two-state model of skin's thermo-mechanical response to superphysiological temperatures.

Kinetics		Waviness			Collagen viscoelasticity		
E _a [J/mol]	A[s ⁻¹]	β _d [-]	$\delta_{\rm d}$ [-]	γ _d [-]	$\mu^{\mathrm{f}}_{\mathrm{d}}$ [MPa]	φ[-]	τ [s]
4.41×10^5	1.59×10^{65}	1.63	0.09	0.79	0.032	8.55	107.7

As a result, the rate of change of the viscous strain follows from solving

$$\left[\frac{\partial^2 W_d^{f,\text{visc}}}{\partial I_4^e \partial I_4^e} I_4^e + \frac{\partial W_d^{f,\text{visc}}}{\partial I_4^e}\right] \dot{I}_4^e = -\frac{1}{\tau} \frac{\partial W_d^{f,\text{visc}}}{\partial I_4^e} I_4^e.$$
(16)

For more details on this hyper-viscoelastic formulation, we refer the reader to Liu et al. [34]. Additionally, the parameters for the two-state model are summarized in Table 2. Note that the parameters for the matrix contribution and the orientation distribution remain unchanged from the intact tissue properties, see Table 1. Furthermore, the parameters in Table 2 are estimated based on previous work on modeling collagen denaturation, e.g. [10,14,20], and further optimized to reproduce quantitatively the observations from Part I [21].

2.2.2. Three-state model

Our second model takes an alternative approach to the above model. While it retains the first element of the above model's second state (i.e., change in stress-free configuration of coiled collagen), it additionally introduces a third state (i.e., second denaturation state). Thus, we first consider an initial stage of denaturation which leads to aforementioned coiling of the collagen molecules, which, we argue, follows from the disassociation of intra-molecular hydrogen bonds within collagen's triple helix [20]. This reaction is, again, driven by a rate k_c of Arrhenius-type with parameters A_c and E_{ac} . However, additionally, we assume that a process of damage (or breakdown) occurs subsequently with a second rate k_b , also of Arrhenius-type with parameters A_b , E_{ab} . This breakdown leads to a reduction in collagen's energy-storage capacity. Thus, as before, let C₀ denote the intact collagen concentration. Additionally, we introduce C_c to denote the concentration of coiled collagen and C_b to capture the damaged collagen concentration. The ODEs describing the kinetics of the three-state model are

$$\dot{C}_{o} = -k_{c}(T)C_{o}$$

$$\dot{C}_{c} = +k_{c}(T)C_{o} - k_{b}(T)C_{c}$$

$$\dot{C}_{b} = +k_{b}(T)C_{c}.$$
(17)

The strain energy of this mixture reads

V

$$V_{\rm d} = W^{\rm m} + C_{\rm o} \int \rho^{\theta} W^{\rm f} d\theta + C_{\rm c} \int \rho^{\theta} W^{\rm f}_{\rm c} d\theta + C_{\rm b} \int \rho^{\theta} W^{\rm f}_{\rm b} d\theta + p[J-1], \qquad (18)$$

where W_c^f and W_b^f are the strain energy contributions due to the fibers after coiling and after being additionally damaged, analogous to Eqs. (4) and (12). Note that these energies are driven by their corresponding shear moduli μ_c^f and μ_b^f , and waviness parameters γ_c and γ_b , respectively. The respective second Piola-Kirchhoff stress tensors for the individual fibers and for skin follow identically to the previous derivations. All parameters for the three-state model – except for those that are identical to intact skin – are summarized in Table 3. As before, some of these parameters are first estimated based on data reported in the literature, e.g., the rate of denaturation, and are then optimized to best match our results from Part I.

Table 3

Parameters for the three-state model of skin's thermo-mechanical response to superphysiological temperatures.

Kinetics				
E _{ac} [J/mol]	$A_{c}[s^{-1}]$	E _{ab} [J/mol]	$A_b[s^{-1}]$	
3.59×10^5	5.21×10^{52}	1.21×10^5	1.25×10^{16}	
Waviness			Collagen Modu	li
$\beta_{\rm c}, \beta_{\rm b}$ [-]	$\delta_{\rm c}, \delta_{\rm b}$ [-]	$\gamma_{\rm c}, \gamma_{\rm b}[-]$	μ_{c} [MPa]	μ_{b} [MPa]
1.63	0.09	0.79	0.318	0.032

2.3. Numerical experiments

To study the response of our two models and to compare them to our experiments, we numerically repeat here the physical experiments described in Part I. That is, we first numerically repeat the isotonic shrinkage experiments at four temperatures. Then, we numerically repeat the isometric biaxial tension experiments. Finally, we numerically repeat the biaxial tensile test experiments comparing the tissue response before and after denaturation. Note that we assume during each experiment that the tissue is in mechanical equilibrium, i.e., $\nabla \cdot \sigma = \mathbf{0}$, where σ is the Cauchy stress. To compute the lateral and cranial stretches during the isotonic shrinkage experiments, we enforce traction-free boundaries. Under the assumption of a homogeneous solution we therefore have zero stresses throughout our domain. Based on these assumptions and the balance of linear momentum we can subsequently solve Eq. (14) for the lateral and cranial (free) stretches λ_x and λ_y . In contrast, to compute the lateral and cranial stresses during the isometric biaxial tension experiments, we compute the stress directly from Eq. (14) assuming that the deformation gradient is equal to the 2nd order identity tensor, or that the stretches in lateral and cranial direction are one. Finally, to compute stresses during the biaxial tensile tests from Eq. (14), we imposed equibiaxial stretches up to 1.18 in both lateral and cranial direction.

3. Results

3.1. Kinetics of denaturation

Starting with the two-state model, under the initial condition $C_0 = 1$, $C_d = 0$, the analytical solution for the denaturation process reads simply as

$$C_{\rm o}(t) = \exp(-k_d t), \ C_{\rm d}(t) = 1 - \exp(-k_d t).$$
 (19)

Solutions to the above equation for temperatures T = 37, 55, 75, 95 °C are shown in Fig. 2A-B. The model with our optimized parameters predicts that denaturation is negligible at T = 37 °C. At T = 55 °C, in contrast, there is marginal decay in C_0 . As we increase the temperature to 75 °C drastic denaturation occurs with all collagen denaturing across the observation period of 100s. As we increase the temperature from 75 °C to 95 °C this process is nearly instantaneous. Figs. 2C-D provide insight into the sensitivity of this process to the parameters of our model. Specifically, they show that increasing the activation energy E_a significantly slows the denaturation process as measured by the time it takes for 50% of collagen to denature (ordinate). Conversely, increasing the rate parameter *A* significantly accelerates the denaturation process as measured, again, by the time it takes for 50% collagen to denature.

The kinetics of the three-state model are more complex, see Fig. 3. Here, the analytical solution for initial conditions $C_0 = 1$, $C_c = 0$, and $C_b = 0$ reads

$$C_0(t) = \exp(-k_c t), \qquad (20)$$



Fig. 2. Denaturation kinetics of the two-state model. A,B) Concentration of intact (C_0) and denatured (C_d) collagen over time upon heat treatment at $T = [37, 55, 75, 95] \circ C$. C,D) Effect of activation energy E_a and maximum rate A on the time it takes to reach half of the denaturation process ($C_0 = 0.5$).

$$C_{\rm c}(t) = \frac{k_c}{k_b - k_c} [\exp(-k_c t) - \exp(-k_b t)], \qquad (21)$$

$$C_{\rm b}(t) = \frac{k_b}{k_c - k_b} \exp(-k_c t) - \frac{k_c}{k_c - k_b} \exp(-k_b t) + 1.$$
 (22)

Note that the decay of the intact collagen follows a similar time evolution as in the two-state model. However, in contrast to the two-state model, the three-state model of course tracks the temporal evolution of two concentrations of denaturing collagens; those of the second (coiled) state and those of the third (damaged) state, see Fig. 3A-C. When heated to T = 75 °C, the coiled collagen con-

centration, C_c , reaches a peak around 10s before decaying as C_b increases, i.e., collagen first coils and then damages. For T = 95 °C, C_c increases almost instantaneously and decays to zero over 100s. In other words, all collagen instantaneously coils, upon which it quickly damages. Fig. 3D-F clarifies the role of the parameters A_b , E_{ab} on the kinetics of the three-state model. An interesting feature of the three-state model is the maximum concentration of coiled collagen C_{cmax} because it, as we will see later, determines the peak in the thermally-induced traction production of skin, viz.

$$C_{\rm c}^{\rm max} = \frac{k_c}{k_b - k_c} \left[\left(\frac{k_c}{k_d} \right)^{\frac{k_c}{k_b - k_c}} - \left(\frac{k_c}{k_d} \right)^{\frac{k_b}{k_b - k_c}} \right],\tag{23}$$



Fig. 3. Denaturation kinetics of the three-state model. A) Concentration of intact (C_o), B) coiled (C_c), and C) damaged (C_b) collagen over time upon heat treatment at $T = 37, 55, 75, 95 \,^{\circ}C$. D) Contour of the maximum value that can be achieved by the coiled collagen concentration C_{cmax} as a function of the secondary activation energy E_{ab} and maximum rate of the secondary reaction A_b . E) Effect of the rate of the second reaction (k_b) on the peak of coiled collagen concentration C_{cmax} . F) Effect of the second reaction rate on the time to reach the peak C_{cmax} as a function of temperature.

with the corresponding time at which the maximum coiled collagen is observed

$$t_{\rm c}^{\rm max} = \frac{\log(k_c) - \log(k_d)}{k_c - k_b}.$$
 (24)

Fig. 3D shows the contour of C_c^{max} as a function of the parameters A_b , E_{ab} which control the second reaction in the threestate model. This contour shows that the peak of coiled collagen is very sensitive to the rate of the second reaction. For the majority of the parameters, the rate of the second reaction is either too slow – such that there is enough time for the native collagen to be converted almost entirely to the coiled state before transitioning to the final state – or too fast – such that there is no coiled collagen accumulation. There is only a narrow band in the A_b , E_{ab} over which the coiled collagen can take intermediate values. Setting $C_{\text{cmax}} = 0.5$ and solving Eqs. (23) and (24), we obtain $k_b = 0.025 \text{ s}^{-1}$. The contour in Fig. 3D then shows the line in the A_b , E_{ab} for $k_b = 0.025s^{-1}$. The other two plots in Fig. 3E-F then show how changes in k_b influence the maximum value of C_c as well as the timing at which this peak occurs for a given temperature.

3.2. Traction-free denaturation

In our first numerical experiments we directly mirror the experiments in Part I of this study by subjecting skin to four temperatures T = 37, 55, 75, 95 °C, in the absence of external tractions. Fig. 4A shows the thermally-induced free shrinkage of skin according to the two-state model, while Fig. 4B shows the results according to the three-state model. In both models, skin

shrinks as the concentration of coiled collagen increases. Mathematically, the transition from native collagen to coiled collagen corresponds to a reduction in each fiber's reference length, thus producing forces that, in the absence of external tractions, lead to shrinkage. Because of the fibers preferential distribution in lateral direction for mouse dorsal skin (i.e., $\hat{\theta}$ of the von Mises distribution equal to zero), forces are larger in that direction, thus leading to anisotropy in the free shrinkage. Following an initial contraction, the two-state model predicts a relaxation step due to the assumed viscoelasticity of the damaged tissue. The threestate model qualitatively predicts a similar, overall behavior. However, rather than being due to viscoelastic recovery as in the twostate model, in the three-state model this relaxation is due to the transition of coiled collagen to damaged collagen. Also, the three-state model predicts shrinkage even for the 55 °C, while the two-state model does not. This difference follows from the significantly larger collagen to matrix stiffness ratio in the threestate model than in the two-state model. Since the properties of the damaged collagen $C_{\rm b}$ in the three-state model are the same as the equilibrium properties of the denatured collagen C_d in the two-state model, both frameworks lead to the same steady state response even though they follow somewhat different paths to equilibrium.

3.3. Isometric denaturation

Again, in accordance with our experiments in Part I of this study, the next numerical experiment explores skin's thermo-



Fig. 4. Traction-free shrinking for the (A) two-state model and (B) the three-state model. Upon subjecting it to temperatures of T = 37, 55, 75, 95 °C, skin shrinks over time. Both models predict that this free shrinkage is anisotropic, with greater deformation in the lateral direction than in the cranial direction. Additionally, both models predict that, after the initial shrinkage, skin also undergoes relaxation during which some of the shrinkage is recovered. In the two-state model this relaxation is due to the assumed viscoelastic behavior of denatured collagen, while in the three-state model this relaxation is due to the continuously accrued damage of the coiled collagen. Note, the shaded regions in Fig. 4 depict the effect of varying the parameter γ of the Weibull distribution describing the fiber waviness, where $\gamma \in [0.71, 0.87]$.

mechanics under isometric heating; that is, while skin's boundaries are fixed. Both the two-state model and the three-state model predict that isometric heating induces tractions that are higher in lateral direction than in cranial direction, see Figs. 5A-B and 6A-B. Moreover, both models predict that those tractions are larger at 95 °C than at 75 °C and that – upon reaching a peak at approximately 10s – those tractions decay and mostly vanish. However, note that the underlying physics are distinctly different. In the two-state model, forces are produced as the denaturing collagen is hindered from coiling, i.e., taking on a shorter reference length, while the subsequent decay follows from the viscoelastic relaxation of the denatured fibers. While the three-state model produces forces similarly as collagen transitions from the first state to the coiled, second state, the force decay mechanism differs. Specifically, in the three-state model the initial peak in force decays as collagen transitions from the coiled, second state, to a damaged, third state.

Fig. 5C-D further explores the effect of critical model parameters of the two-state model: The parameter ϕ in Eq. (13) controls the scaling of the dissipative branch in the viscoelastic model. Consequently, this parameter mostly influences the peak stress in Fig. 5A-B. In contrast, the parameter τ in Eq. (15) controls the



Fig. 5. The two-state model predicts that skin produces tractions under isometric conditions and exposure to superphysiological temperatures. After an initial peak, those tractions decay and eventually mostly vanish. A-D) Effect of the parameter ϕ and τ of the two-state model at A,C) 75 °C and B,D) 95 °C, respectively, see Eq. (13). Note, the shaded regions correspond to variations in the parameters as noted at the top of each figure.

timescale of stress relaxation. Thus, it primarily controls the decay time.

Fig. 6C-D similarly explores the effect of critical model parameters of the three-state model. The peak and decay of the stress are primarily influenced by the modulus of the coiled collagen, μ_c , and the second reaction maximum rate, A_b , between the coiled, second state and the damaged, third state.

3.4. Biaxial mechanics following thermal denaturation

In the last numerical experiment we test skin's constitutive response to 10s of thermal loading at 90 °C. Specifically, we

compare skin's biaxial mechanics before and after heat treatment. We thereby, once again, mimic our experimental protocol in Part I of this study. Both, the two-state model and the three-state model, predict that skin's mechanics fundamentally change during denaturation, see Fig. 7A-B for the results of both models, respectively. While skin's biaxial response remains anisotropic, it changes from its classic J-shape – or strain-stiffening – behavior to a near-linear behavior. With this transformation, skin's stiffness at small stretches increases, while it decreases at large stretches. The underlying microstructural mechanisms are, in-fact, identical between the two models. That is, in both models the shift in the stress-free length of collagen molecules towards a shorter



Fig. 6. The three-state model predicts that skin produces tractions under isometric conditions and exposure to superphysiological temperatures. As with the two-state model, after an initial peak, those tractions decay and eventually mostly vanish A-D) Effect of the coiled collagen stiffness parameter μ_c and the reaction rate k_b between the coiled collagen and damaged collagen of the three-state model at A,C) 75 °C and B,D) 95 °C, respectively. Note, the shaded regions correspond to variations in the parameters as noted at the top of each figure.

reference length shifts the "activation" or "uncrimping" length of collagen to smaller stretches; thus, increasing stiffness at small stretches. Simultaneously, coiled collagen is endowed with smaller shear moduli; thus, reducing stiffness at larger stretches.

4. Discussion

In our current work we propose two competing models to capture the thermo-mechanical response of skin to superphysiological temperatures. This work was motivated by a lack of modeling and simulation tools that could explain our observations in Part I of this study that: i) skin shrinks anisotropically when heated under isotonic traction-free conditions, ii) skin generates anisotropic tractions when denaturing under isometric, or fixed-boundary, conditions, and iii) when heated, skin changes its biaxial constitutive response to become more linear, with a stiffness increase at small stretches and a stiffness decrease at large stretches [21]. Our models build upon existing evidence that skin's thermo-mechanical response to superphysiological loading is driven by collagen denaturation that follows Arrhenius-like kinetics [22]. Additionally, they are built on the knowledge that denatured collagen changes its stress-free reference configuration and that collagen changes its mechanical properties upon denaturation [20]. Our first, two-state model accounts for skin's response through a transition from a first, native state to a second state in which collagen coils, i.e., takes a shorter stress-free configuration, and in which collagen transforms from a hyperelastic material to a hyper-viscoelastic material. In our three-state model, the second state also leads to coiling of collagen, i.e. reduced reference length, but does not lead to a transition to a hyper-viscoelastic material. Instead, in our three-



Fig. 7. Biaxial properties of skin after 10s of denaturation at 90°C, for the two-state model (A), and the three-state model (B). In both cases, denaturation leads to a stiffening at small strains but softening at larger strains. Note, the shaded regions correspond to variations in stiffness parameters for the two- and three-state models. For the two-state model, the stiffness of the denatured collagen was varied in the range $\mu_d \in [0.025, 0.038]$ MPa. For the three-state model, the stiffness of the coiled collagen was varied in the range $\mu_c \in [0.25, 0.38]$ MPa.

state model, a third state leads to collagen damage through which its ability to store strain energy is compromised.

4.1. Modeling success

In a first step toward modeling skin's thermo-mechanics, we established a microstructurally-inspired hyperelastic model of skin's native behavior. This baseline model builds on an explicit consideration of skin's primary structural constituent: collagen. Specifically, we model collagen's orientation and waviness according to probability density functions [29,36]. This approach has successfully captured the anisotropy - via collagen's orientation distribution - and the nonlinear stiffening behavior - via collagen's waviness distributions - of other collageneous tissues such as arteries and thrombus [29,37]. Among the advantages of this approach over other approaches, such as the projection of stress from the fiber network onto one or two structural tensors [23,28], is our ability to bestow collagen fibers with microscopy-based measurements of orientation and waviness [32]. Our work shows that this modeling approach successfully captures all salient features of skin's experimentally observed, biaxial constitutive behavior. That is, our model accurately captures native skin's anisotropy and strain-stiffening behavior (see Supplemental Figures S1, S2). Note, in key figures we also visualized the sensitivity of our model predictions to key parameters to illustrate the potential impact of subjects-specific variations.

Our two models of skin's thermo-mechanical response to superphysiological loading share the same intact skin model. However, they differ by their accounting for a set of observations made in Part I of this study. Regardless of approach, numerical experiments with both models reproduce all of our physical experiments. In the first numerical experiment, our models correctly predict that skin minimally shrinks under traction-free conditions when exposed to temperatures of 37 °C or 55 °C, but drastically shrinks when exposed to temperatures of 75 °C and 95 °C. Interestingly, both models predict that, after an initial monotonic phase of shrinkage, skin expands again, a phenomenon that we did not identify in our experiments. The mechanisms underlying this late expansion differ between the two models. In our twostate model, the late expansion of skin is due to collagen's transition to a hyper-viscoelastic material. In other words, after collagen coiling produces sufficient internal tractions to lead to shrinkage, these stresses then viscoelastically relax as strain energy dissipates. In our three-state model, the late expansion of skin is due to collagen's transition from the second, coiled state to the third, damaged state of collagen. In other words, shrinkage follows from collagen coiling and build-up of internal tractions, while its late expansion results from a loss in collagen's capacity to retain those internal tractions while it is becoming increasingly damaged. While this relaxation presents a deviation from our experiments, we believe that this discrepancy may be due to the large experimental uncertainty in our measurements. In other words, we submit that this relaxation behavior may have been present but hidden in the experimental noise. Future work in which we longitudinally observe the time-dependent shrinkage of samples may reduce this noise and confirm our models' predictions.

In the second numerical experiment, our models accurately predict that skin produces tractions when its boundaries are fixed and it is subjected to 75 °C and 95 °C. Moreover, both models predict that those tractions rapidly decay after reaching a temperaturedependent peak. The traction production in both models stems from the transition of skin's collagen from a native state to a coiled state. In other words, as collagen's reference configuration becomes shorter, fixed boundaries lead to an induction of strain energy and thus tractions. However, both models differ in how they capture the subsequent decay. In the two-state model, the decay is due to viscoelastic relaxation of collagen. On the other hand, the threestate model captures the decay via collagen damage. In both models, the direction-dependence of the traction peak stems from the relatively higher distribution of collagen in the lateral direction than in the cranial direction for mouse dorsal skin. Also in both models, the temperature-dependence of the traction peak is due to the temperature-accelerated coiling of collagen relative to the characteristic time of each model's respective decay mechanism.

In the third numerical experiment, we compared skin's constitutive response before and after being exposed to 10s of 90 °C. Here, again, both models predict our experimentally observed phenomena. Specifically, both models correctly predict that skin transitions from a J-shaped, strain-stiffening constitutive behavior to a (mostly) linear constitutive behavior. That is, skin becomes stiffer at small stretches and less stiff at large stretches. In contrast to previous phenomena where the underlying mechanisms between the two-state model and the three-state model differed fundamentally, they don't in this experiment. The reason being that the relatively short exposure to superphysiological loading of 10s leads to skin's response in both models being governed primarily by collagen coiling. For example, in the two-state model the viscoelastic time constant τ is 107s. In other words, after 10s of exposure collagen's behavior is still primarily hyperelastic. Similarly, the reaction rate of the three-state model that governs the transition from the second to the third state results in there being a small fraction of collagen in the damaged state at 10s, see Fig. 3. Consequently, both models predict the temperature-induced change in constitutive behavior based on collagen coiling and the associated reduction in collagen's stress-free configuration and stiffness.

Please note that we described our modeling success primarily in gualitative terms. The reason lies in our motivation to test our models' basic, mechanistic-assumptions rather than to perfectly calibrate our models. However, to ensure that our models are also capable of capturing our quantitative data, we did calibrate the parameters of our models to match our experimental data from Part I, see Supplemental Figures S3-S8. Please note that we calibrated our parameters through a hybrid approach in which we informed those parameters that were not affected by denaturation with mechanical and imaging data from our previous work and from the data in Part I [32]. For example, we informed the fiber waviness and orientation distributions of the native tissue directly via measurements on two-photon images, see Supplemental Figures S1, S2. On the other hand, we identified those parameters that were directly involved in predicting skin's response to thermal denaturation through an optimization procedure that minimized the error between the model's predictions and our experiments. Those parameters include, for example, the stress-free fiber length and the stiffness parameters of both models. As per the Supplemental Figures, our model predictions fit our experimental findings not only qualitatively but also quantitatively.

4.2. Limitations and future work

While both of our models are based on microstructural and molecular considerations, they don't capture the molecular scale directly. Further numerical - and experimental - work on the molecular scale is needed to test our proposed mechanisms and to refine our predictions at the tissue level. Potential molecularscale numerical methods that have previously been applied are coarse-grained methods, statistical mechanics, or molecular dynamics by Stylianopoulos et al., Miles et al., Yeo et al., and Mlyniec et al. [20,38-40]. Such simulations may provide additional insight into the main mechanisms driving our models, such as collagen coiling, damage, and inter-fibril sliding. Thereby, they may shed light, at least theoretically, onto which model is more accurate and also inform future experiments. Moreover, future experiments should interrogate denatured skin's response to repeated testing. Because damage is non-reversible while viscoelastic effects are, these experiments may provide the necessary insight into which model more closely reflects skins denaturation biophysics; See Figure S9 for the two-state models' response to stress relaxation and cyclic loading for example [34]. Beyond our lack of molecular insight, another significant limitation of our work is the reduction of the present thermo-mechanical problem to a homogeneous one. For example, we ignore heat transfer phenomena and assume instantaneous thermal equilibrium. In reality, the transfer of heat from the reservoir to the tissue may not be instantaneous, and there are likely gradients of temperature between the edge and the center of the tissue. We justify neglecting these spatial effects with our samples' small dimensions of approximately $10mm \times 10mm \times 1mm$. Nevertheless, additional work is necessary to test these assumptions - for example following the framework outlined by McBride et al. [41]. We also made simplifying assumptions about the constitution and constitutive behavior of skin. That is, we ignored native skin's viscoelasticity/poroelasticity, heterogeneous composition, and we assumed that the tissue behaved incompressibly without testing this assumption explicitly [42-45]. We did not consider more complex interactions such as a potential coupling between loading and thermal stability [46], or that the thermo-mechanical response may also be driven by other proteins, specifically elastin. Here, again, future work will have to explore these protein's relative contribution to skin's thermo-mechanical response to superphysiological loading. Finally, the models developed here are valid only in the range of temperatures over which we compared them to experiment data; that is, between 37 and 95 °C.

5. Conclusion

In our current work we propose and compare two models that link the kinetics of collagen denaturation to skin's coupled thermomechanical response under superphysiological temperatures. Both models capture all experimental tissue-level observations that we made in Part I of this study. Because both models fundamentally differ in their underlying microstructural and molecular mechanisms, they may inform future experiments that could test each of the models' assumptions. Additionally, our models may be used predictively. Therefore, our models are a crucial step toward a deeper understanding of thermal skin injuries and toward the rational, model-based design of skin's – and other collageneous tissues'– thermal treatments.

Author Contributions

William Meador designed and conducted all experiments, coauthored the manuscript. John Toaquiza Tubon developed the mathematical framework of native skin mechanics and co-authored the manuscript. Omar Moreno-Flores developed the mathematical framework of native skin mechanics and co-authored the manuscript. Adrian Buganza Tepole designed the experiments, developed the mathematical framework, conducted all simulations, and co-authored the manuscript. Manuel Rausch designed the experiments, developed the mathematical framework, and coauthored the manuscript.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Supplementary material

The code needed to reproduce all the figures in this paper can be found at https://github.com/abuganza/skin_thermomechanics_model.

Supplementary material associated with this article can be found in the online version, at doi:10.1016/j.actbio.2021.11.031.

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